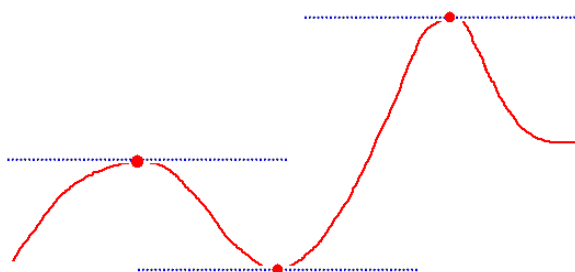


Section 2.2 – The Derivative as a Function

The Derivative as a Function:

- Recall that we defined $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$.
- Of course, this limit must exist to work properly.
- If the limit exists at $x = a$, then the function is said to be _____ at $x = a$.
- If the limit exists on some interval (specifically, for all values within that interval) then the function is said to be _____.
- If the limit exists for all values in its domain, then the function is said to be _____. This is the same concept as continuous, where if no point or interval is given, you assume it means everywhere.
- So long as the limit definition above exists, it can be interpreted as a function itself, and it is useful to help us understand the behavior of $f(x)$.
- There are several other symbols used for the derivative of a function, including $f'(x) = \frac{df}{dx} = \frac{d}{dx} f(x) = Df(x) = D_x f(x)$.
- Of course, if the function is not f , say it is $y(x)$, then the above definitions would change accordingly.

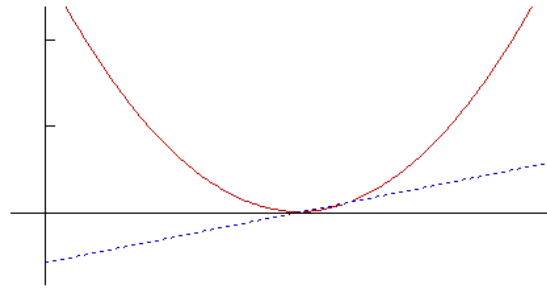
Critical Points:



- Q** What do you notice about the tangent lines given in the above picture?
A: _____.
- Q:** What is so special about these points?
A: _____.
- We will cover this in more detail later, but the above points are examples of _____, or points where the derivative is zero or undefined. Above, these critical points have a first derivative of zero.
- You can ‘match’ a graph of a function with its derivative by looking at the critical points, whenever you have a critical point on your original function, the derivative function will be zero (or undefined) there.

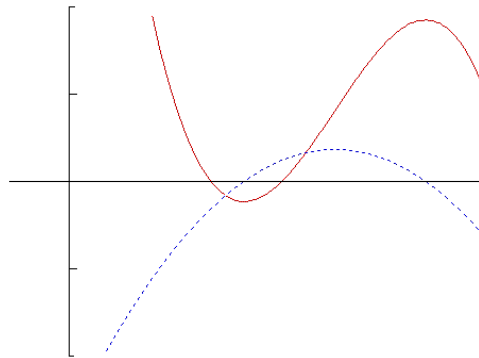
- Q: Can you identify which is the original function and which is the derivative?

A: _____
_____.



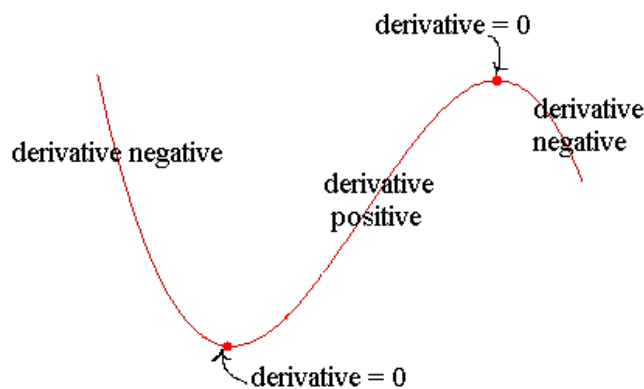
- Q: Can you identify which is the original function and which is the derivative?

A: _____
_____.



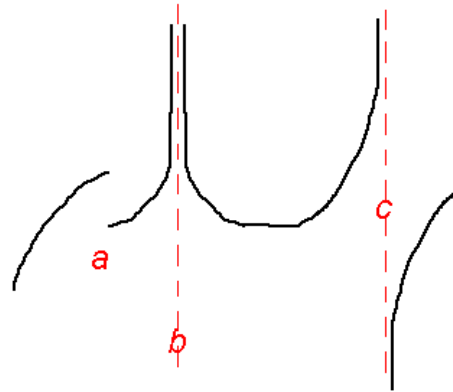
Sign of the derivative:

- When a function is increasing, the slope of the tangent lines will be positive, hence the derivative is _____ when a function is _____.
- In a similar manner, the derivative is _____ when a function is _____.
- When a function changes from increasing to decreasing, you have a _____, where the derivative _____.



What Can Go Wrong:

- Recall the requirements for continuity.
- If a function is not continuous, then it cannot be differentiable. So the following is not differentiable at the values a , b and c .



- Differentiability is actually more strict than continuity.
- Any sharp corners will not be differentiable



- Also, there may be places where the function has a vertical tangent.

